# **QoS Adaption aware Algorithm for Grid Service Selection**

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#### **Abstract**

Grid service composition has been recognized as a flexible way for resource sharing and application integration since appearance of service-oriented architecture. Approaches are needed to select service candidates with various Quality of Service (QoS) levels according to use's performance requirements. In this paper We model this problem as the Multi-Constrained Optimal Path Selection Problem (MCOP), due to the dynamic property of grid service, adaptive mechanism is introduced to ensure the whole QoS when some service candidates fail. An algorithm QAGSS is proposed. Simulation results show that QAGSS has greater success rate and lower cost than previous algorithms.

**Keywords:** Grid, QoS adaptation, Composite service, DAG, MCOP.

#### 1. Introduction

Open Grid Service Architecture (OGSA) [1] as a Service Oriented Architecture (SOA) provides a combination framework, in which physical resources are virtualized to the user in the form of grid services. Grid services use standard interfaces for invoking. Using standard interfaces individual services can be combined into a composite service, by which complicated application can be completed. Since many services have the same functional properties while different non-functional properties, such as QoS, cost etc. and service-oriented grid requires deliver seamless QoS, so algorithms that can rapidly and efficiently select service candidates to form a composite service for applications is needed.

Candidates of composite service and their relationship can be represented by directed acyclic graph (DAG), in which QoS and cost can be seen as weight. Hence the problem above can be modeled as MCOP, which is to select a suitable path satisfying multi-constraints meanwhile minimizing the global cost. Algorithms for solving MCOP are introduced to web services selection problem in many previous. Different

from web service, the state of grid service varies dramatically. Existing services may change QoS level, fail or even withdraw at any moment, while new services may join. In this case, adaptive mechanism is worth being considered for QoS level assurance. In this paper, we model the problem as MCOP and an effective algorithm QAGSS is proposed, which takes QoS adaption into account.

The rest of this paper is organized as follows. In Section 2 we will present a brief overview of related work about QoS and service selection. We introduce an approach for QoS parameters standardization in Section 3. The details about algorithm will be narrated and discussed in Section 4. In Section 5 experiment results are presented, and we make a brief analysis. Finally, the paper is concluded in Section 6 and future work is also discussed here.

## 2. Related work

Foster etc. propose GARA in [2]. GARA supports reservation and adaptation, which support the management of end-to-end QoS in service-oriented grid environment. This is the initial work on grid architecture to support QoS. Rashid Al-Ali proposed a Grid-QoS management framework (G-QoSM) [3], in this framework Rashid etc. classify services into three types based on different QoS levels: guaranteed, controlled load and best effort. Adaption strategies are used to support resource capacity sharing [4].

QoS parameters are classified into five categories and a hierarchical structure of grid QoS is proposed in [5]. The heuristic algorithm based on the structure is confirmed to be effectively by experiment results, but algorithm considered no composite service as well as the cost it takes.

T. Yu etc. study the end-to-end QoS issues of composite service by using a QoS broker in [6]. The problem is modeled in two ways: the combinatorial model defines the problem as a Multi-dimension Multi-choice Knapsack Problem (MMKP) and the graph model defines the problem as a Multi-Constrained Optimal Path Problem(MCOP) and novel algorithms are designed to meet the global QoS constraints while maximize the user defined utility function. These

algorithms can solve the problem by finding near optimal solutions in polynomial time, and it is proved to be suitable for web services, but due to the dynamic nature of grid service, whether it is adapt to grid service is still need to be confirmed.

Composite service selection is modeled as MCOP Problem, for one dimension of QoS, the MCOP Problem is known as NP-complete [10]. To cope with this problem, many pseudo-polynomial-time algorithms such as jaffe's algorithm [8] are proposed, but their complexities depend both on the actual values of the edge and scale of the problem. An efficient heuristic algorithm is introduced in [7] to minimize the nonlinear cost function for finding a feasible path while also incorporating the cost optimization of the selected feasible path, however, the complexity of computation will increase as  $\mu$  increases, and here  $\mu$  is an adjustable parameter used to calculate the cost function in algorithm. In this paper we improve this algorithm by introducing upper bound of u to reduce the computational complexity. It is proved that the time complexity of QAGSS proposed in this paper is the same as that of Dijkstra's algorithm [9].

# 3. QoS parameter standardization

OoS describes a service's capability to meet consumer's demands. There are many properties to describe QoS, such as concurrent processing capabilities, throughput, duration, reliability, availability, accuracy, security, and so on. The performance of service can be reflected by these parameters from different perspectives, which can be roughly classified into additive and non-additive. For the additive parameters such as duration, throughput it is the sum of the additive parameter value from end to end. In contrast, value with respect to a non-additive parameter, such as bandwidth is determined by the value of that constraint at the bottleneck part. For constraints associated with non-additive parameters, we can simply remove services that do not satisfy these constraints. So in this paper we will mainly discuss additive QoS parameters. The user's QoS requirements may be different with parameters, for example, user may demand delay less than 5ms, while throughput no less than 100, also different service classes may have different quantification standards for the same QoS parameter. Hence, we present an approach to standardize QoS parameters. We assume that m is the number of service classes and n is the dimension of QoS,  $q_k(i)$  represent the *i*th dimension QoS parameter of service class  $S_i$ , all QoS parameters are positive, so we get a n\*m matrix as follow:

$$\begin{pmatrix} q_1(1) & \dots & q_1(m) \\ \vdots & \ddots & \vdots \\ q_n(1) & \dots & q_n(m) \end{pmatrix}$$

We roughly put parameters into positive criterion and negative criterion. Positive criterion donates the higher value the higher quality such as throughput, while negative criterion donates the lower value the higher quality such as duration. In this paper two approaches are provided respectively to both criteria.

Translation approach for parameters belongs to positive criterion is shown in equation (1):

$$Q_{k}(i) = \begin{cases} q_{k}(i) / \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)}, & \text{if } \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)} \neq 0 \\ 0, & \text{if } \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)} = 0 \end{cases}$$
(1)

Translation approach for parameters belongs to negative criterion is shown in equation (2):

$$Q_{k}(i) = \begin{cases} \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)} / q_{k}(i), & \text{if } \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)} \neq 0 \\ 0, & \text{if } \sqrt{\sum_{i=1}^{m} q_{k}^{2}(i)} = 0 \end{cases}$$
 (2)

We can simply define QoS constraint relationship r(q, u), it is a binary relationship, the first one of the pair indicates service QoS parameter, the target service value user expected is represented by the other. There is only one element in the set of constraint relationship:  $R=\{\geq\}$ .

# 4. QoS Adaption aware Algorithm

### 4.1. Service composition model

The services we discussed can be divided into various service class based on functionality, a service class is a set of services with common functionality but different non-functional properties such as QoS levels and costs etc. The services requested by a user or application can be classified into two categories individual service and composite service, the first one means request can be accomplished by a single service class while the other implies request should be completed by a set of service classes. DAG composite service shown in Figure 1 is a general kind of composite service described by DAG, in which node represents service class and directed edge represents collaborative relationship among service classes. DAG composite service has several execution paths, pipeline composite service is one of them, so it can be considered as special case of DAG composite service, and in this paper we discuss DAG composite service for general purpose. Each service class may have many candidate services, and each service has its own QoS level, but users do not care about it, usually they put forward end-to-end QoS requirements. Consequently, the problem need to be solved by service selection is how to select a feasible and optimal path from a mass of candidate ones in Figure 2 to achieve the user's QoS requirements meanwhile minimize costs.

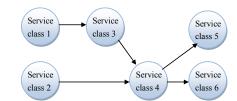


Figure 1. DAG Composite Service

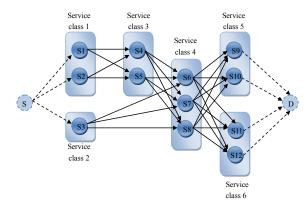


Figure 2. Service Candidate Graph

In Figure 2 we add two nodes—source node and destination node, from source node S we draw edges to all nodes that do not have predecessors, in the same way from all nodes that do not have subsequences we draw edges to destination node D. Each candidate represented by a node has its own QoS parameter values and cost, here we give an approach to move QoS parameter values and costs from nodes to edges, and definition is shown as follows:

**Definition 1** Consider a composite service that is represented by DAG graph G=(V, E), where V is the set of nodes and E is the set of edges. e(i, j) donates the directed edge (si, sj), each edge is associated with n additive QoS parameters  $e_k(i, j)$  and cost c(i, j), k=1,2,...,n.

$$e_{k}(i,j) = \begin{cases} (Q_{k}(i) + Q_{k}(j))/2, & \text{if } (si \neq S, sj \neq D) \\ Q_{k}(i) + Q_{k}(j)/2, & \text{if } (si = S, sj \neq D) \\ Q_{k}(i)/2 + Q_{k}(j), & \text{if } (si \neq S, sj = D) \end{cases}$$

$$c(i,j) = \begin{cases} (c(i) + c(j))/2, & \text{if } (si \neq S, sj \neq D) \\ c(i) + c(j)/2, & \text{if } (si = S, sj \neq D) \\ c(i)/2 + c(j), & \text{if } (si \neq S, sj = D) \end{cases}$$

$$(4)$$

in Figure 2 the both nodes S and D are added without QoS parameters and costs, so we can set n parameter values and costs of both nodes are zeros. Hence, we model service selection problem as MCOP using  $e_k(i, j)$  as QoS parameters c(i, j) as costs respectively instead of  $Q_k(i)$  and c(i), the definition is given below:

**Definition 2** MCOP: Consider a composite service that is represented by DAG graph G = (V, E), where V is the set of nodes and E is the set of edges. Each edge is associated with n additive QoS parameters  $e_k(i, j)$  and c(i, j), k = 1, 2, ..., n. Given n constraints  $u_k$ , k = 1, 2, ..., n, the problem is to find a path p from source node S to

destination node D subject to:

(i) 
$$e_k(p) = \sum_{e(i,j) \in p} e_k(i,j) \ge u_k$$
 for  $k = 1,2,...,n$ , and

(ii) 
$$c(p) = \sum_{e(i,j) \in p} c(i,j)$$
 is minimized over all

feasible paths satisfying (i).

For a path p the sum of values of nodes that belong to p equals to that of edges belong to p, and the values include QoS parameter values and costs.

$$c(p) = \sum_{e(i,j)\in p} c(i,j) = \sum_{si\in p} c(i)$$

$$e_k(p) = \sum_{e(i,j) \in p} e_k(i,j) = \sum_{si \in p} Q_k(i)$$

## 4.2. Introduction to the QAGSS Algorithm

From above definitions, we now present the following cost function  $C_{\mu}(p)$  for the service selection problem:

$$C_{\mu}(p) = \left(\frac{u_1}{e_1(p)}\right)^{\mu} + \left(\frac{u_2}{e_2(p)}\right)^{\mu} + \dots + \left(\frac{u_n}{e_n(p)}\right)^{\mu}$$
 (5)

where  $\mu \geq 1$ . Then we conclude the following conclusions on the performance of algorithm that return a path p by minimizing the cost function (5) for a given  $\mu \geq 1$ .

**Theorem 1** Suppose that there is at least one feasible path exists, and p is a path that minimizes the cost function  $C_{\mu}(p)$  for a given  $\mu \ge 1$ . Then

- (i)  $u_k \le e_k(p)$  for at least one k
- (ii)  $e_{\iota}(p) \ge \sqrt[\mu]{n}u_{\iota}$  for all other k's
- (iii) The likelihood of finding a feasible path increases as  $\mu$  increases.

Proof of Theorem 1in detail can be found in [7]. Now we present our heuristic algorithm QAGSS, which is composed of three parts, one is feasible part, second is optimal part and last is adaptive part. For the feasible part, QAGSS tries to minimize the objective function  $C_{\mu}$  for  $\mu \geq 1$ . It first finds optimal path from each node x to D using function Reverse Dijkstra [9] with some modifications to relaxation process, then it starts from S and discovers each node based on the minimization of  $C_{\mu}(p)$ , where p is a complete path passing through node x. This path is determined heuristically at node x by connecting the already traveled segment from S to x and the remaining segment from x to D, and this can be done by calling function Look Ahead Dijkstra [9] also with some modifications to relaxation process in [7]. The main QAGSS algorithm is described as follows, and Table 1 shows the description of variables algorithm used.

> Main QAGSS Algorithm Input: G=(V, E), S, D, u Output: A suitable composite service 1 Reverse\_Dijkstra (G, e, D)

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2 If (t[S]>n) then
3 return failure
4 End If
5 μ ← MAX_NUM
6 Look_Ahead_Dijkstra (G, e, c, S)
7 If (H<sub>k</sub>[x] ≥ u<sub>k</sub> for k∈ [1,n]) then
8 return suitable composite service S<sub>sui</sub>
9 Ada_Set (S<sub>sui</sub>)
10 End If
11 return failure
```

Table 1. Description of variables

Variable	Description
t[x]	The cost of the shortest path from x to D
	under the cost function $C_{\mu}(p)$
$T_k[x]$	The individually accumulated edge values
	along the path
$P_t[x]$	Predecessor of x on optimal path that from
	x to D
C[x]	The cost of a foreseen complete path via
	node x based on the cost function $C_{\mu}(p)$
$H_k[x]$	The individually accumulated edge values
	along the already traveled segment of the
	path from S to x
$P_{C}[x]$	Predecessor of x on the path from S to x
c[x]	The cost along the already traveled
	segment of the path from S to x
u	The set of $u_k$ , $k \in [1,n]$

There are two directions in the algorithm, backward from S to D and forward from D to S. The backward direction is depicted by lines 1-4 in QAGSS, which estimate the cost of the remaining segment using  $\mu = 1$ . Reverse Dijkstra returns a path p from S to D. Before moving to forward direction, QAGSS checks whether t[S]>n or not, if true it means no feasible path exist, which is based on Theorem 1. If not true, path p may be a feasible path. If path p is feasible, we use Look Ahead Dijkstra to find a path q with condition  $c(q) \le c(p)$ , if not we use it to find a path q with condition  $C_{\mu}(q) \leq C_{\mu}(p)$ , in both cases, we set  $\mu$  as MAX NUM that is a constant we set in the algorithm, which could be changed to alter the possibility of finding a feasible path. This is based on Theorem 2 described as follows:

**Theorem 2** Suppose Reverse\_Dijkstra returns path p, and Look\_Ahead\_Dijkstra returns path q, then

- (i) if p is feasible, q is feasible too and  $c(q) \le c(p)$
- (ii) if p is not feasible,  $C_{\mu}(q) \leq C_{\mu}(p)$ .

Proof in detail can also be found in [7], and the following is relaxation process of Reverse\_Dijkstra:

**Reverse\_Dijstra\_Relax Input:** Two nodes 
$$x, y \in V$$
**Output:** Predecessor of  $y$  on the path
$$1 \quad \text{If } \left( \frac{u_k}{t[x]} > \sum_{k=1}^n \left( \frac{u_k}{T_k[y]} + \frac{u_k}{e_k(x,y)} \right) \right) \text{ then}$$

2 
$$t[x] \leftarrow \sum_{k=1}^{n} \left( \frac{u_k}{T_k[y]} + \frac{u_k}{e_k(x,y)} \right)$$
  
3  $T_k[x] \leftarrow T_k[y] + e_k(x,y)$  for  $k \in [1,n]$   
4  $P_t[y] \leftarrow x$   
5 **End If**

In forward direction, QAGSS invokes  $Look\_Ahead\_Dijkstra$  to identify if there is another path q which possibly improves the performance over path p.

# $Look\_Ahead\_Dijkstra\_Relax$

**Input:** Two nodes  $x, y \in V$ 

Output: Predecessor of y on the path and accumulated cost

1 Set t as a temporary node

 $2 \quad c[t] \leftarrow c[x] + c(x, y)$ 

$$3 \qquad C[t] \leftarrow \sum_{k=1}^{n} \left( \frac{u_k}{H_k[x]} + \frac{u_k}{e_k(x,y)} + \frac{u_k}{T_k[y]} \right)^{\mu}$$

4  $H_k[t] \leftarrow H_k[x] + e_k(x, y)$  for  $k \in [1,n]$ 

5  $T_k[t] \leftarrow T_k[y]$  for  $k \in [1,n]$ 

6 If (Select\_best (t, y) = t) then

7  $c[y] \leftarrow c[t]$ 

 $C[y] \leftarrow C[t]$ 

9  $H_k[y] \leftarrow H_k[t]$  for  $k \in [1,n]$ 

10  $P_C[y] \leftarrow x$ 

11 **End If** 

8

The above function firstly judge the value of  $\mu$ , if  $\mu$ =1 it is no need to compute cost function  $C_{\mu}$ , otherwise use  $C_{\mu}$  with  $\mu$  = MAX\_NUM to select feasible path. Then we use function Select\_best to choose the next node for performance improvement. It selects one of input nodes such that the selected one should minimize cost if foreseen complete path passing through these nodes are feasible, otherwise, it selects one that minimizes the cost function  $C_{\mu}$ .

#### Ada\_Set

**Input:** Suitable composite service S<sub>sui</sub>

**Output:** Adaptive service set  $SC_i$ : the *i*th service class in  $S_{sui}$   $S_i$ : the *j*th one in *l* candidates

 $S_g$ : the selected candidate in a service class

A<sub>i</sub>: the backup service set of SC<sub>i</sub>

1 **For** each  $SC_i$  in  $S_{sui}$ 

2 If  $(S_g \in A_i)$  then

3 remove S<sub>g</sub> from A<sub>i</sub>

4 End If

5 **If**  $(Q_k(g) \ge Q_k(A_i) \text{ for } k \in [1,n])$  **then** 

6 find l candidates  $\in$  SC<sub>i</sub> subject to  $Q_k(j) \ge Q_k(g)$  for  $j \in [1,l]$   $k \in [1,n]$  and cost are low

7 For each S<sub>j</sub>

8 If  $S_i \neq NULL$  then

 $9 \qquad \text{ Add } S_j \text{ to } A_i$ 

10 **End If** 

- 11 End For
- 12 End If
- 13 End For

For the enhancement of service adaptive capacity, function Ada\_Set is designed. It reserves a backup service set for every service class on the path. Whenever a suitable path is found, Ada\_Set is called to find l candidates subject to  $Q_k(j) \geq Q_k(g)$  for  $j \in [1,l]$   $k \in [1,n]$  and cost are low, and add these to  $A_i$ . The intention of setting up  $A_i$  is to compensate for changing or failure of selected services. When QAGSS find suitable path, it can select candidates from backup service set, after a suitable path is found, Ada\_Set check whether a backup service is on the path, if true remove it

The QAGSS algorithm determines whether there is possibility of path existence by invoking function Reverse\_Dijkstra. If true continues to invoke function Look\_Ahead\_Dijkstra to find a more suitable path. Ada\_Set is introduced for assurance of end-to-end QoS in grid environment. Since the modified Dijkstra's algorithm is executed two times at most, the QAGSS algorithm has the same time and space complexities with Dijkstra.

### 5. Experiment

#### 5.1. Configuration

In this paper we conduct the simulation experiment to estimate the performance of QAGSS algorithm we proposed, and compare it with jaffe's algorithm [8] which is used to solve the MCP problem. MCP problem is a slightly different version of MCOP problem, aims only at finding feasible path that satisfies multiconstraints. For more than two dimensions MCP problem is known to be NP-complete. In [8] the author considers 2-dimension MCP problem, and uses Dijkstra's shortest path algorithm with two adjustable parameters  $\alpha$ ,  $\beta$  to minimize objective function. Simulation arrangement is described below.

In the simulation, we use a Request\_generator to generate user's requests, which is composed of service classes included and corresponding QoS constraints. The number of service classes in each request is classified into two groups [1, 5] and [5, 10]. For brevity, we define that every service class has 10 candidates, QoS dimension is 2 and capacity of backup set is 1. So the number of candidate nodes in DAG also has two ranges [10, 50] and [50, 100]. Each node has 2-dimension QoS parameters and cost information, we use Node\_inf\_generator to generate these values respectively. Without loss of generality, every dimension QoS parameters are generated by different distributions, and mean of each dimension QoS parameters are calculated. We use these mean instead of

edge mean to evaluate the average value of a path, as equation (6) shows:  $A_k = (Nsc/2)*m_k$  (6)  $A_k$  represents the kth dimension average value of a path, Nsc is the average of service classes included in a request, so the average length of a path can be represented by expression Nsc/2 and  $m_k$  describes the kth dimension QoS parameters mean. The QoS levels of requests have significant effect on the performance. For comparison of performance under different situations, we divided the QoS requests into three groups:

- (i) 75% QoS request  $c_k$  smaller than average value  $A_k$  for  $k \in [1,n]$
- (ii) 50% QoS request  $c_k$  smaller than average value  $A_k$  for  $k \in [1,n]$
- (iii) 25% QoS request  $c_k$  smaller than average value  $A_k$  for  $k \in [1,n]$

In each group, we divide requests into two groups, one with range from 1 to 5 service classes and the other with range from 5 to 10. For each group the simulation is repeated 100 times respectively and the results reported in the subsequent sections are average values.

### 5.2. Results and Analysis

In Figure 3 the cost of composite service selected by QAGSS is lower than Jaffe's, since QAGSS algorithm requires at most two iterations of Dijkstra's algorithm while jaffe's requires one. The cost of path returned by second iteration is no larger than that of first. Success rate in equation (7) is introduced to make contrast between different algorithms under different situations.

Success rate = number of requests satisfied / total number of requests (7)

From Figure 4 we conclude that success rate improves as MAX\_NUM increases, especially among the range from 1 to 10, which is consistent with theorem 1. When MAX\_NUM exceeds 10, there is little improvement in success rate. It is due to the nature of the heuristic algorithm, one can expect few anomalies in the general trend. We also observe the smaller the number of service classes included in a request the greater success rate is. Contrast between Jaffe's algorithm and QAGSS algorithm is described in Figure 5. It is obviously that success rate of ours is larger than that of jaffe's. QAGSS execute in two directions, when path returned from backward direction is not feasible, it

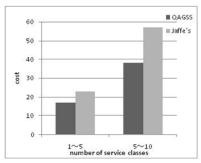


Figure 3. Cost returned by QAGSS and Jaffe's

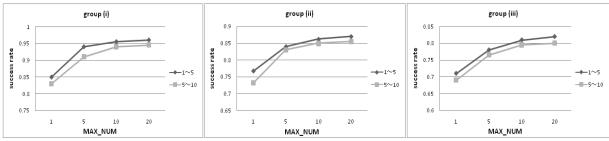


Figure 4. The success rate performance of QAGSS with MAX\_NUM

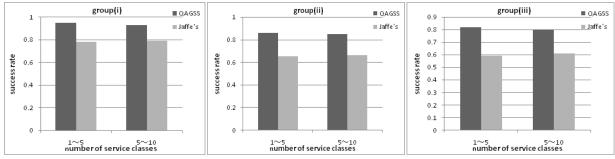


Figure 5. Success rate performance of QAGSS and Jaffe's

will continue to move to forward direction if there exist possibility. According to theorem 2(ii) cost function may be minimized, then increases success possibility.

#### 6. Conclusion and Future work

This paper studies composite service selection problem in grid environment. QoS classification is discussed briefly and approach for standardization is also provided. We model the problem as MCOP, and then QAGSS algorithm is proposed to select least cost composite service while satisfying end-to-end QoS requirements. Adaptive mechanism is considered in QAGSS to adapt to the dynamic characteristic of grid service. In addition, QAGSS has the same time complexity with Dijkstra's, which is suitable for making runtime decisions. Experiment results show that QAGSS performs better among similar algorithms in success rate and cost.

In future, we plan to investigate performances of QAGSS in large-scale distributed grid environment. We will also make some improvements on adaptive mechanism to achieve higher performances and to be more suitable for grid services selection.

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